989. Dipole Moments, and Sorption Characteristics at the Solution-Solid Interface of a Series of Substituted Azobenzenes.

By D. A. IBBITSON, T. JACKSON, (MISS) A. MCCARTHY, and C. W. STONE.

Sorption of a series of substituted azobenzenes from benzene on activated alumina has been studied, and evidence provided that hydrogen-bond formation is responsible for the sorption process. From the isotherm data, standard thermodynamic free-energy changes have been calculated, and it is apparent that hydroxyazobenzenes have a greater affinity for the alumina surface than p-aminoazobenzene. Sorption saturation values are explained in terms of size and orientation of the sorbate molecules, and it is suggested that hydroxyazobenzenes may be sorbed on different surface sites from aminoazobenzenes. The apparent dipole moments of the azo-compounds in benzene and dioxan have been determined from measurements on dilute solutions, but no correlation between $\Delta \mu$ and free-energy decrease on sorption is observed. That the dipole moments of 2-hydroxy-5-methylazobenzene in benzene and dioxan are almost the same is considered to be evidence of intramolecular hydrogen bonding in this compound. Dipole moments of the azo-compounds in benzene are compared with those of the corresponding benzene derivatives, and explained by the difference in the +M effect of the amino- and the hydroxy-group.

THIS investigation was carried out to determine if thermodynamic free-energy decrease on sorption at the solution-solid interface is reflected in the dipole moments of the sorbates.

Sorption of a series of substituted azobenzenes from benzene on activated alumina has been studied, and standard free-energy decreases associated with the sorption process have been evaluated. Dipole moments of the sorbates in benzene and dioxan have also been determined.

Of the sorbates used, the monosubstituted compounds are of interest in that they have been used ^{1,2} in determining an arbitrary gradation of activities of chromatographic alumina. It was expected that these compounds would exhibit wide variation of polarity and sorptive affinity for alumina. Benzene was chosen as solvent for the sorption study because of its non-polar character. In the light of Kiselev's work,³ however, it appears that, although non-polar, benzene does not show the lowest interactions with oxide surfaces. For example, the sorption and heat of sorption of benzene on hydrated silica are higher than those of hexane, owing to additional interactions with the acid hydroxyl groups of the sorbent surface.

EXPERIMENTAL

(1) Sorption Studies.—(a) Materials. Chromatographic alumina, passing a 120-mesh B.S. sieve, was stored in bulk; 2.0 g, portions were dried at 110° for 48 hr. before use in the sorption experiments. Preliminary experiments indicated that drying of the alumina to constant

- ¹ Brockmann and Schodder, Ber., 1941, 74, 73.
- ² Brockmann, Discuss. Faraday Soc., 1949, 7, 58.
 ³ Kiselev, 2nd Internat. Congress of Surface Activity, "Solid/Gas Interface," Butterworths Scientific Publ., London, 1957, p. 179.

weight was complete after 48 hr. at 110° , and resulted in a 1.5% loss in weight, due presumably to removal of adsorbed moisture.

Benzene, dried over sodium wire, was distilled, and the fraction of b. p. $80 \cdot 1^{\circ}/760$ mm. was collected.

p-Aminoazobenzene, recrystallised from alcohol, had m. p. 124°. p-Hydroxyazobenzene, prepared in the normal manner, was recrystallised from acetic acid and then alcohol, and had m. p. 153°. p-Methoxyazobenzene, prepared by treating p-hydroxyazobenzene with dimethyl sulphate in alkaline solution at 60°, was recrystallised from acetic acid and then alcohol, and had m. p. 55°. p-Acetamidoazobenzene, m. p. 146°, and p-acetoxyazobenzene, m. p. 88°, prepared by acetylation, were recrystallised from alcohol. p-Dimethylaminoazobenzene, prepared by coupling diazotised aniline with dimethylaniline in acid solution, was recrystallised from alcohol and had m. p. 118°. 4-Hydroxy-3-methyl-, m. p. 129°, 4-hydroxy-2-methyl-, m. p. 105°, and 2-hydroxy-5-methyl-azobenzene, m. p. 108°, were prepared by the normal coupling process and recrystallised from alcohol.

(b) Method of sorption. The sorption experiments were carried out at 35° as previously described ⁴ except that equilibrium concentrations were determined on a Hilger Spekker photoelectric absorptiometer.

(c) Sorption results. For the sorption process, free sorbate molecules + vacant sites = occupied sites, if all sites are identical and there is no sorbate interaction, then $K = \theta/(1 - \theta)c$, it being assumed that the activity coefficients of the occupied and unoccupied sites are the same. θ is the fraction of surface covered, c is the concentration of the free sorbate molecules in the mobile phase (in mole l.⁻¹), an activity coefficient of unity being assumed, and K is an equilibrium constant for sorption. This equation can be rewritten in the form $\theta = Kc/(1 + Kc)$, which

. .

.

-

a ...

	I AB	ELE I. S	orption a	nd free-er	nergy dat	<i>a</i> .			
		p-]	Hydroxya	zobenzene					
	$10^4 x_1 = 2$	·97; 10 ⁻⁴	K = 0.64;	$-\Delta G^{\circ} =$	5400 cal.	mole ⁻¹ .			
10 ⁴ c	2.03	7.66	18.23	35 .06	49.89				
$10^4 x_0$	1.840	2.330	2.695	$2 \cdot 895$	3.145				
		4-Hvdr	oxv-3-met	hvlazoben	zene				
	$10^{4}r_{1} - 2$	·12· 10-47	7 - 0.49	$-\Lambda G^{\circ} -$	5200 cal	mole-1			
104c	5.94	6.60	8.30	10.30	14.15	16.08			
$10^{4}x_{0}$	1.435	1.532	1.691	1.775	1.855	1.885			
v		4 TT 1	9						
		4-Hydr	oxy-2-met	nylazoben	zene				
1.04	$10^4 x_1 = 2$	$\cdot 21; 10^{-4}$	x = 2.51;	$-\Delta G^{\circ} =$	6200 cal.	mole ⁻¹ .			
10 ⁴ <i>c</i>	0.98	1.22	1.790	2.31	3.30	4.31			
10-20	1.990	1.020	1.790	1.920	1.990	2.009			
		2-Hydr	oxy-5-met	hylazoben	zene				
	$10^4 x_1 = 0$	•41; 10 ⁻⁴ I	$X = 2 \cdot 28;$	$-\Delta G^{\circ} =$	6100 cal.	mole ⁻¹ .			
10 ⁴ c	0.24	0.38	0.60	0.91	1.33	2.39	3.42		
$10^4 x_0$	0.118	0.165	0.221	0.283	0.323	0.353	0.361		
p-Acetoxyazobenzene									
$10^4 x_1 = 1.66$; $10^{-4} K = 1.51$; $-\Delta G^{\circ} = 5900$ cal. mole ⁻¹ .									
104c	$1 \cdot 31$	3.00	4.63	10.00	18.52	37.86			
$10^4 x_0$	1.218	1.375	1.447	1.550	1.608	1.636			
Ū									
		Þ	·Aminoazo	ob enze ne					
	$10^4 x_1 = 0$	$\cdot 67; 10^{-4}$	K=0.06;	$-\Delta G^{\circ} =$	3900 cal.	mole ⁻¹ .			
10 ⁴ c	5.15	13.27	17.00	20.00	$23 \cdot 81$	30.00	36.37	50.85	
$10^4 x_0$	0.123	0.296	0.345	0.375	0.408	0.444	0.469	0.480	
		<i>p</i> -A	cetamidoa	zobenzene	e				
	$10^4 x_1 = 0$	$.61: 10^{-4}F$	X = 0.58	$-\Delta G^{\circ} =$	5300 cal.	mole ⁻¹ .			
10 ⁴ c	2.12	5.00	- 8·50	15.09	26.79	38.79			
$10^4 x_0$	0.261	0.405	0.495	0.560	0.575	0.584			

⁴ Erić, Goode, and Ibbitson, J., 1960, 55.

is the familiar Langmuir isotherm. On replacement of θ by x_0/x_1 , where $x_0 =$ moles of solute sorbed per g. of alumina at equilibrium, and $x_1 =$ moles sorbed at saturation, the Langmuir equation is transposed to give $c/x_0 = 1/x_1K + c/x_1$. This equation was found to be applicable to the sorption data in Table 1, and by measurement of the slopes and intercepts of the plots of c/x_0 against c, x_1 , and K were calculated for each sorbate. The standard free-energy of sorption, $-\Delta G^0$, was calculated from equation $-\Delta G^0 = \mathbf{R}T \ln K$, this quantity providing a measure of the strength of the sorption bond. Sorption and free-energy data are presented in Table 1.

(2) Dipole Moments.—(a) Materials. Dioxan was repeatedly refluxed with sodium, and then fractionally distilled under anhydrous conditions.

(b) Apparatus and methods. Dielectric constants and refractive indices of solutions of graded concentrations of each sorbate in benzene and dioxan were determined at 25.0° . The apparatus and methods used were the same as in a previous investigation,⁴ and the results are summarised in Table 2, where the symbols have their usual significance.

100w	ε	$n_{\mathbf{D}}$	100w	ε	$n_{\rm D}$	100w	ε	$n_{\rm D}$	100w	ε	$n_{\rm D}$	
p-An	ninoazob	enzene	p-Am	inoazobe	enzene	p-Hyd	roxyazoł	oenzene	p-Hyd	roxyazol	benzene	
īi	in benzer	ne	-	in dioxa	n	i	n benzer	ıe		in dioxa	n	
0.000	2.2725	1.4981	0.000	$2 \cdot 2063$	1.4200	0.000	2.2725	1.4981	0.000	2.2138	1.4201	
0.118	2.2776	1.4985	0.096	$2 \cdot 2132$	1.4202	0.093	2.2742	1.4982	0.198	$2 \cdot 2209$	1.4206	
0.227	2.2821	1.4988	0.190	2.2198	1.4206	0.181	2.2764	1.4984	0.292	2.2241		
0.342	$2 \cdot 2871$	1.4992	0.286	2.2267	1.4209	0.270	2.2782	1.4986	0.393	2.2276	1.4211	
0.447	2.2916	1.4995	0.382	$2 \cdot 2329$	terran ca	0.361	2.2799	1.4987	0.584	$2 \cdot 2343$	1.4218	
0.556	$2 \cdot 2963$	1.4999	0.478	$2 \cdot 2391$	1.4218	0.452	$2 \cdot 2820$	1.4989	0.770	$2 \cdot 2414$	1.4222	
4-Hyd	lroxy-3-1	nethyl-	4-Hyd	lroxy-3-r	nethyl-	4-Hyd	lroxy-2-r	nethyl-	4-Hyd	roxy-2-1	methyl-	
azober	izene in j	benzene	azobe	nzene in	dioxan	azober	izene in l	benzene	azober	azobenzene in dioxan		
0.000	2.2725	1.4981	0.000	2.2115	1.4200	0.000	2.2725	1.4981	0.000	2.2128	1.4200	
0.227	$2 \cdot 2767$	1.4986	0.192		1.4206	0.215	2.2768	1.4985	0.195	2.2188	1.4206	
0.451	$2 \cdot 2807$	1.4991	0.382	2.2255	1.4213	0.444	$2 \cdot 2815$	1.4988	0.392	$2 \cdot 2249$	1.4213	
0.676	$2 \cdot 2850$	1.4995	0.579	$2 \cdot 2325$	1.4220	0.547	$2 \cdot 2838$	1.4991	0.507	2.2285	1.4217	
0.898	$2 \cdot 2893$	1.5000	0.767	$2 \cdot 2398$	1.4226	0.658	2.2858	1.4993	0.602	2.2316	1.4220	
1.128	$2 \cdot 2937$	1.5005	0.960	$2 \cdot 2460$	1.4232	0.872	$2 \cdot 2900$	1.4996	0.790	2.2373	1.4226	
2-Hvd	lroxy-5-1	nethvl-	2-Hvc	lroxv-5-r	nethvl-	⊅-Met	hoxvazol	enzene	⊅-Metl	noxvazol	benzene	
azober	izene in	benzene	azobe	nzene in	dioxan	i	n benzer	ie	1	in dioxa	n	
0.000	2.2725	1.4981	0.000	2.2133	1.4200	0.000	2.2725	1.4981	0.000	$2 \cdot 2091$	1.4200	
0.216	2.2755	1.4985	0.182	$2 \cdot 2165$	1.4205	0.092	$2 \cdot 2742$	1.4982	0.194	$2 \cdot 2129$	1.4202	
0.440	$2 \cdot 2786$	1.4989	0.374	$2 \cdot 2195$	1.4210	0.181	2.2758	1.4984	0.384	$2 \cdot 2167$	1.4206	
0.663	2.2817	1.4993	0.567	2.2228	1.4215	0.272	$2 \cdot 2776$	1.4986	0.482	$2 \cdot 2186$	1.4207	
0.886	$2 \cdot 2846$	1.4997	0.760	$2 \cdot 2263$	1.4219	0.361	$2 \cdot 2790$	1.4987	0.577	$2 \cdot 2204$	1.4209	
						0.452	2.2808	1.4989	0.769	$2 \cdot 2242$	1.4213	
p-Dimethylaminoazo- p-Acetamidoazo-		<i>p</i> -Ace	<i>p</i> -Acetoxyazobenzene									
benzene in benzene benzene in benzene			- i	n benzer	ne							
0.000	2.2725	1.4981	0.000	2.2725	1.4981	0.000	2.2725	1.4981				
0.115	$2 \cdot 2790$	1.4983	0.114	$2 \cdot 2814$	1.4982	0.123	2.2744	1.4982				
0.230	$2 \cdot 2859$	1.4986	0.183	$2 \cdot 2865$	1.4984	0.225	$2 \cdot 2760$	1.4983				
0.345	$2 \cdot 2922$	1.4989	0.224	$2 \cdot 2898$		0.340	2.2778	1.4985				
0.453	$2 \cdot 2978$	1.4992	0.226	$2 \cdot 2901$	1.4985	0.453	2.2796	1.4986				
0.562	$2 \cdot 3041$	1.4994	0.340	$2 \cdot 2990$	1.4987	0.566	$2 \cdot 2815$	1.4987				

TABLE 2.

The molar orientation polarisation at infinite dilution, $P_{2\infty}$, and the dipole moment, μ , of each azobenzene derivative were calculated from equations (1) and (2) respectively,

$$P_{2\infty} = 3M_2 v_1 \{ \alpha / (\varepsilon_1 + 2)^2 - \nu / (n_1^2 + 2)^2 \} \quad . \quad . \quad . \quad . \quad (1)$$

$$\mu := 0.012812 \ (P_{2\infty} \times T)^{\frac{1}{2}} \quad . \quad . \quad . \quad . \quad . \quad . \quad (2)$$

 M_2 = molecular weight of solute; v_1 , ε_1 , and n_1 are specific volume, dielectric constant, and refractive index respectively of the solvent at $25 \cdot 0^\circ$; $\alpha = (d\varepsilon/dw)_{w=0}$, $\mathbf{v} = (d\pi^2/dw)_{w=0}$. α and \mathbf{v} were determined from the limiting slopes of the plots of ε against w, and n_2^p against w.

8 c

DISCUSSION

Polarisation and sorption data are summarised in Table 3.

In the present work, although alumina was slightly coloured after standing in contact with solutions of azobenzene in benzene, the extent of sorption was not measurable.⁵ This confirms that the main source of affinity between the sorbates used and the alumina surface is in the polar substituent groups. Evidence that hydrogen bonding is primarily responsible for sorption of non-ionic solutes on alumina is available from a number of sources.^{6,7} p-Methoxyazobenzene and p-dimethylaminoazobenzene are not sorbed by the alumina used in this investigation, and it is evident from the data in Table 3 that, with the exception of p-acetoxyazobenzene, only those compounds containing substituent groups capable of hydrogen bonding with the sorbent surface are sorbed with a measurable free-energy decrease. From a study of the influence of proton-accepting solutes on the surface film properties of cetyl acetate, Allingham, Giles, and Neustädter⁸ obtained evidence of intermolecular hydrogen bonding, the acetate group acting as proton donor. These authors suggest that hydrogen bonding occurs through a hydrogen atom of the methyl residue in the acetyl group which is activated by the adjacent carbonyl-oxygen

	IA	IBLE 0.	F 01	urisuiio	n unu	sorpiion u aia.		
Azobenzenc				$P_{2^{\infty}}$		$-\Delta G^{\circ}$		Previous *
deriv.	Solv.*	10 ³ α	$10^2 \nu$	(c.c.)	μ (D)	(cal. mole ⁻¹)	$10^{4}x_{1}$	values of μ (D)
p-Amino-	в	4246	98	120.3	$2 \cdot 43$	3900	0.67	B 15·4° 2·71,ª
*	D	6920	102	188.8	3.04			B 2.48 b
<i>p</i> -Hydroxy-	в	2090	56	56.7	1.66	5400	2.97	B 14·7° 1·62,ª
	D	3557	78	87.9	2.07			D 15·2° 2·04 a
4-Hydroxy-3-methyl-	в	1882	64	49 ·0	1.55	5200	$2 \cdot 12$	
	\mathbf{D}	3631	93	91·1	$2 \cdot 11$			
4-Hydroxy-2-methyl-	\mathbf{B}	2022	55	58.4	1.69	6200	$2 \cdot 21$	
	D	3094	92	$72 \cdot 3$	1.88			
2-Hydroxy-5-methyl-	\mathbf{B}	1347	54	$32 \cdot 1$	1.25	6100	0.41	
	\mathbf{D}	1702	73	$31 \cdot 2$	1.23			
p-Methoxy-	в	1877	58	51.3	1.58		-	В 22·8° 1·29 «
	D	1965	49	49.4	1.55			
p-Dimethylamino-	в	5602	71	206.8	3.18			B 26.9° 3.68,"
								B 25° 3.22^{11}
<i>p</i> -Acetamido-	\mathbf{B}	7826	57	$326 \cdot 2$	3.99	5300	0.61	
p-Acetoxy-	в	1568	3 6	54.3	1.63	5900	1.66	

Polarisation and sorbion data TADLE 2

* B = benzene; D = dioxan.

^a Bergmann and Weizmann, Trans. Faraday Soc., 1936, **32**, 1318. ^b Campbell, McAllister, and Rogers, J. Amer. Chem. Soc., 1953, **75**, 864. Other refs. as in text.

atom. A similar mechanism may operate in the sorption of p-acetoxyazobenzene on alumina, the sorbate acting as proton donor. Alternatively, the acetyl group may act as the acceptor group in hydrogen bonding, with the alumina surface as proton donor.

The affinity of p-hydroxyazobenzene for the alumina surface is appreciably greater than that of p-aminoazobenzene, indicating that the hydroxyl group forms stronger bonds than the amino-group. Although it is rather surprising that $-\Delta G^0$ for p-acetoxyazobenzene is greater than that for p-hydroxyazobenzene, the result is consistent with the high $-\Delta G^0$ value for p-acetamidoazobenzene in comparison with the value for p-aminoazobenzene, *i.e.*, replacement of a hydrogen atom of a hydroxy- or amino-group by the acetyl group causes an increase in $-\Delta G^0$.

Of the disubstituted azobenzenes examined, it is noteworthy that the dipole moment of 2-hydroxy-5-methylazobenzene is almost the same in benzene as in dioxan, indicating the presence of intramolecular hydrogen bonding in this compound. Hoyer ' concludes

⁵ Jackson, M.Sc. Thesis, Leeds, 1958.

⁶ Cummings, Garren, Giles, Rahman, Sneddon, and Stewart, J., 1959, 535; Giles, Mehta, Stewart, and Subramanian, J., 1954, 4360. ⁷ Hoyer, Kolloid-Z., 1951, **121**, 121.

⁸ Allingham, Giles, and Neustädter, Discuss. Faraday Soc., 1954, 16, 92.

that the sorption of simple non-ionic anthraquinones and azo-compounds on alumina columns (judged by speed of travel) is weaker when any amino-, hydroxy-, etc., groups they contain are internally chelated, than when they are free. The relatively high value of $-\Delta G^0$ (6100 cal. mole⁻¹) for 2-hydroxy-5-methylazobenzene does not appear to confirm this conclusion.

The previously determined x_1 value for phenol (4.59×10^{-4}) indicates almost complete unimolecular coverage of the alumina surface.⁴ Increased cross-sectional area of the azobenzene molecule, and surface-area requirements of the acetoxy- and methyl groups are suggested as factors responsible for the smaller x_1 values of p-hydroxyazobenzene and its derivatives. Sorption of 2-hydroxy-5-methylazobenzene through the hydroxyl group in the 2-position would produce a tilted arrangement of molecules on the sorbent surface, and the consequently increased surface-area requirements of the sorbed molecules may explain the very small x_1 value of this compound.

A marked difference exists between the sorption saturation values of the hydroxyand amino-azobenzenes, and two explanations appear possible. First, it could be argued that both types of compound are sorbed by the same sites, the hydroxyl group forming stronger bonds with the sorbent surface than the amino-group. Since the availability of suitable sites, and the dimensions of the sorbate molecules, also determine the extent of surface saturation, and since the surface requirements of the hydroxy- and aminogroups are not very different, it is possible that the two types of compound are sorbed on different surface sites. Unfortunately, no evidence is available that the alumina surface is, in fact, heterogeneous.

Table 3 indicates that the dipole moment of the sorbate determined in either benzene or dioxan is unrelated to free-energy decrease on sorption. In agreement with other workers,⁹ it is found that in the case of those compounds capable of hydrogen bonding through the hydrogen atom of the hydroxy- or amino-group and the oxygen atom of the dioxan molecule, the dipole moments determined in dioxan are all greater than those in benzene. It was expected that $\Delta \mu (\mu_D - \mu_B)$ would be parallel with free-energy changes on sorption, but such is not the case, and it seems more likely that variations in the magnitude of the O-H or N-H bond moment on sorption may be significant in interpreting variations in sorption affinity. This appears to be so from a study of dipole moments, and sorption affinity for alumina, of a series of substituted phenols.⁴

The dipole moments of the compounds studied are of interest. A comparison of the data in Table 4 shows that the moments of the hydroxyazobenzenes do not differ greatly

		TABLE 4.			
Substituent	4- OH	4-OMe	4-OAc	4-OH, 3-Me	4-OH, 2-Me
μ (D) (azobenzene deriv.) μ (D) (benzene deriv.)	1∙66 1∙54 ¢	1.58 1.30 b	1·63 1·52 ¢	1.55 1.44 ^d	1.69 1.60 d
Substituent	2-OH, 5-Me	$4-NH_2$	$4\text{-}\mathrm{NMe}_2$	4-NHAc	
μ (D) (azobenzene deriv.) μ (D) (benzene deriv.)	1·25 1·57 ª	2·43 1·51 ^{9 b}	3·18 1·58 95	3.99 4.01 €	

^a Goode and Ibbitson, J., 1960, 4265. ^b Le Fèvre, "Dipole Moments," Methuen, London, 1953, p. 134. ^e Donle, Z. phys. Chem., 1931, 14, B, 326. ^d Williams, Phys. Z., 1928, 29, 683. ^e Le Fèvre and Le Fèvre, J., 1936, 1130.

from those of the corresponding benzene derivatives, indicating the absence of *cis*-isomers in the former compounds (dipole moments of cis- and trans-azobenzene are 3.0 D and zero, respectively ¹⁰). Also the increased length of the conjugated system in the hydroxyazobenzenes would appear to have very little effect on the mesomeric electron release of the hydroxyl group. Campbell, Young, and Rogers 11 suggest, however, that it is just this

¹¹ Campbell, Young, and Rogers, J. Amer. Chem. Soc., 1951, 73, 5789.

^{* (}a) Vassiliev and Syrkin, Acta Physicochim. U.R.S.S., 1941, 14, 414; (b) Few and Smith, J., 1949, 753; (c) idem, ibid., p. 2663; (d) Smith, J., 1950, 3532; (e) idem, J., 1953, 109; (f) Smith and Walshaw, J., 1957, 3217.
 ¹⁰ Hartley and Le Fèvre, J., 1939, 531.

type of electron interaction which accounts for the increased dipole moments of p-aminoand p-dimethylamino-azobenzene as compared with aniline and dimethylaniline respectively. The greater difference found for the dimethylamino-group (1.60 D) may be due to electron release from the two methyl groups attached to the nitrogen atom and hence to the conjugated system. Interaction on a smaller scale would be expected in the case of hydroxyl and methoxyl groups in view of the sequence NH₂ > OMe > OH for the mesomeric electron release from these groups (+M effect). The dipole moments of p-acetamidoazobenzene and acetanilide are almost identical, indicating that the acetyl group decreases the mesomeric interaction between the nitrogen p-electrons and the azolink or distant benzene ring.

The authors are indebted to J. Hall for assistance in the preparation and purification of the compounds, to N. W. Vale for the construction of the heterodyne-beat apparatus, and to the Chemical Society for a grant for the purchase of dioxan. They also thank Dr. A. G. Catchpole and Dr. J. W. Smith for valuable discussions.

DERBY AND DISTRICT COLLEGE OF TECHNOLOGY.

[Received, May 5th, 1960.]